# Package: stagedtrees (via r-universe)

September 13, 2024

Type Package
Title Staged Event Trees

Version 2.3.0

Description Creates and fits staged event tree probability models, which are probabilistic graphical models capable of representing asymmetric conditional independence statements for categorical variables. Includes functions to create, plot and fit staged event trees from data, as well as many efficient structure learning algorithms. References: Carli F, Leonelli M, Riccomagno E, Varando G (2022). <doi:10.18637/jss.v102.i06>. Collazo R. A., Görgen C. and Smith J. Q. (2018, ISBN:9781498729604). Görgen C., Bigatti A., Riccomagno E. and Smith J. Q. (2018) <arXiv:1705.09457>. Thwaites P. A., Smith, J. Q. (2017) <arXiv:1510.00186>. Barclay L. M., Hutton J. L. and Smith J. Q. (2013) <doi:10.1016/j.ijar.2013.05.006>. Smith J. Q. and Anderson P. E. (2008) <doi:10.1016/j.artint.2007.05.004>.

License MIT + file LICENSE

Encoding UTF-8
LazyData true
RoxygenNote 7.3.1

**Roxygen** list(markdown = TRUE)

 ${\bf URL} \ {\tt https://github.com/stagedtrees/stagedtrees}$ 

BugReports https://github.com/stagedtrees/stagedtrees/issues

**Imports** stats, graphics, cli, rlang, matrixStats

**Suggests** testthat (>= 3.0.0), bnlearn, covr, clue, igraph

Config/testthat/edition 3

**Depends** R (>= 2.10)

Repository https://stagedtrees.r-universe.dev

RemoteUrl https://github.com/stagedtrees/stagedtrees

RemoteRef HEAD

**RemoteSha** b2c58485fbd06c608fb92619d51539ead4b7ac1b

2 Contents

## **Contents**

s.character.parentslist	 •	3
Asym		4
s_adj_matrix		5
s_bn		5
s_parentslist		6
ıs_sevt		7
parplot.sevt		8
eg		9
id		10
ri_matrices		11
compare_stages		11
confint.sevt		13
covid_patients		15
lepsubtree		17
ull_indep		18
generate_linear_dataset		20
generate_random_dataset		21
generate_xor_dataset		21
get_stage		22
graph-conversion		23
nclusions_stages		25
oin_positions		26
oin_unobserved		26
ogLik.sevt		27
r_test		28
PhDArticles		29
olot.ceg		30
olot.sevt		31
Pokemon		33
oredict.sevt		34
orint.sevt		35
orob		36
andom_parentslist		37
andom_sevt		38
ename_stage		39
ample_from		40
earch_best		40
earch_greedy		41
evt		42
evt_add		44
evt_df		45
evt_fit		45
evt_nvar		46
evt_simplify		47
evt_varnames		48
tagedtrees		48

```
65
Index
70
```

as.character.parentslist

Print a parentslist object

#### **Description**

Nice print of a parentslist object

## Usage

```
## S3 method for class 'parentslist'
as.character(x, only_parents = FALSE, ...)
## S3 method for class 'parentslist'
print(x, ...)
```

## **Arguments**

```
x an object of class parentslist.only_parents logical, if the basic DAG encoding is to be returned.additional arguments for compatibility.
```

#### Value

as.character.parentslist returns a string encoding the associated directed graph and eventually the context specific independences. The encoding is similar to the one returned by modelstring in package **bnlearn** and package **deal**. In particular, parents of a variable can be enclosed in:

• ( ) if a partial (conditional) independence is present.

4 Asym

- { } if a context specific independence is present.
- <> if no context specific and partial (conditional) independences are present, but at least a local independence is detected.

If a parent is not enclosed in parenthesis the dependence is full.

If only\_parents = TRUE, the simple DAG encoding as in **bnlearn** is returned.

## **Examples**

```
model <- stages_hclust(full(Titanic), k = 2)
pl <- as_parentslist(model)
pl
as.character(pl)
as.character(pl, only_parents = TRUE)</pre>
```

Asym

Asym dataset

## **Description**

Artificial dataset with observations from four variables having a non-symmetrical conditional independence structure.

## Usage

Asym

#### **Format**

A data frame with 1000 observations of 4 binary variables.

#### Source

The data has been generated by Federico Carli <carli@dima.unige>.

as\_adj\_matrix 5

as\_adj\_matrix

Convert to an adjacency matrix

## **Description**

Convert to an adjacency matrix

## Usage

```
as_adj_matrix(x, ...)
## S3 method for class 'parentslist'
as_adj_matrix(x, ...)
## S3 method for class 'ceg'
as_adj_matrix(x, ignore = x$name_unobserved, endnode = TRUE, ...)
```

## Arguments

x an R object... additional parametersignore list of stages to be ignored.

endnode logical value. If TRUE a final node fil be added.

## Value

the equivalent adjacency matrix for as\_adj\_matrix.ceg: the adj matrix corresponding to the CEG.

as\_bn

Convert to a bnlearn object

## **Description**

Convert a staged tree object into an object of class bn from the **bnlearn** package.

## Usage

```
as_bn(x)
## S3 method for class 'parentslist'
as_bn(x)
## S3 method for class 'sevt'
as_bn(x)
```

6 as\_parentslist

## Arguments

x an R object of class sevt or parentslist.

#### Value

an object of class bn from package bnlearn.

as\_parentslist

Obtain the equivalent DAG as list of parents

## **Description**

Convert to the equivalent representation as list of parents.

## Usage

```
as_parentslist(x, ...)
## S3 method for class 'bn'
as_parentslist(x, order = NULL, ...)
## S3 method for class 'bn.fit'
as_parentslist(x, order = NULL, ...)
## S3 method for class 'sevt'
as_parentslist(x, silent = FALSE, ...)
```

## **Arguments**

x an R object.

... additional parameters.

order of the variables, usually a topological order.

silent if function should be silent.

#### **Details**

The output of this function is an object of class parentslist which is one of the possible encoding for a directed graph. This is mainly an internal class and its specification can be changed in the future. For example, now it may also include information on the sample space of the variables and the context/partial/local independences.

In as\_parentslist.sevt, if a context-specific or a local-partial independence is detected a message is printed (if silent = FALSE) and the minimal super-model is returned.

as\_sevt 7

#### Value

An object of class parentslist for which a print method exists. Basically a list with one entries for each variable with fields:

- parents The parents of the variable.
- context Where context independences are detected.
- partial Where partial independences are detected.
- local Where no context/partial independences are detected, but local independences are present.
- values values for the variable.

#### See Also

print.parentslist and as.character.parentslist for the parenthesis-encoding of the DAG structure and the asymmetric independences.

## **Examples**

```
model <- stages_hclust(full(Titanic), k = 2)
pl <- as_parentslist(model)
pl$Age</pre>
```

as\_sevt

Coerce to sevt

## Description

Convert to an equivalent object of class sevt.

## Usage

```
as_sevt(x, ...)
## S3 method for class 'bn.fit'
as_sevt(x, order = NULL, ...)
## S3 method for class 'bn'
as_sevt(x, order = NULL, values = NULL, ...)
## S3 method for class 'parentslist'
as_sevt(x, order = NULL, values = NULL, ...)
```

## **Arguments**

```
x an R object.
```

... additional parameters to be used by specific methods.

order order of the variables.

values the values for each variable, the sample space.

8 barplot.sevt

#### **Details**

In as\_sevt.bn.fit the order argument, if provided, must be a topological order of the bn.fit object (no check is performed). If the order is not provided a topological order will be used (the one returned by bnlearn::node.ordering).

In as\_sevt.parentslist the order argument, if provided, must be a topological order of the corresponding DAG (no check is performed). If the order is not provided names(x) is used.

The values parameter is used to specify the sample space of each variable. For a parentslist object created with as\_parentslist from an object of class sevt, it is, usually, not needed to specify the values parameter, since the sample space is saved in the parentslist object.

#### Value

the equivalent object of class sevt.

#### **Examples**

```
model <- stages_hclust(full(Titanic), k = 2)
plot(model)
pl <- as_parentslist(model)
model2 <- as_sevt(pl)
plot(model2) ## this is a super-model of the first staged tree
## we can check it with
inclusions_stages(model, model2)</pre>
```

barplot.sevt

Bar plots of stage probabilities

#### **Description**

Create a bar plot visualizing probabilities associated to the different stages of a variable in a staged event tree.

#### Usage

```
## S3 method for class 'sevt'
barplot(
  height,
  var,
  ignore = height$name_unobserved,
  beside = TRUE,
  horiz = FALSE,
  legend.text = FALSE,
  col = NULL,
  xlab = ifelse(horiz, "probability", NA),
  ylab = ifelse(!horiz, "probability", NA),
  ...
)
```

ceg 9

## Arguments

height an object of class sevt.

var name of a variable in object.

ignore vector of stages which will be ignored and left untouched, by default the name

of the unobserved stages stored in object\$name\_unobserved.

beside a logical value. See barplot. horiz a logical value. See barplot.

legend.text logical.

col color mapping for the stages, see col argument in plot.sevt.

xlab a label for the x axis. ylab a label for the y axis.

... additional arguments passed to barplot.

## Value

As barplot: A numeric vector (or matrix, when beside = TRUE), giving the coordinates of all the bar midpoints drawn, useful for adding to the graph.

## **Examples**

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
barplot(model, "Kids", beside = TRUE)</pre>
```

ceg

Chain event graph (CEG)

## Description

Build the CEG representation from an object of class sevt.

## Usage

```
ceg(object)
```

## Arguments

object an object of class sevt.

#### **Details**

An object of class ceg is a staged event tree object with additional information on the positions.

#### Value

an object of class ceg.

10 cid

## **Examples**

```
DD <- generate_xor_dataset(3, 100)
model <- stages_bhc(full(DD))
model.ceg <- ceg(model)
model.ceg$positions</pre>
```

cid

Context specific interventional discrepancy

## Description

Compute the context specific interventional discrepeancy of a staged tree with respect to a reference staged tree.

## Usage

```
cid(object1, object2, FUN = mean)
```

## **Arguments**

object1 an object of class sevt. object2 an object of class sevt.

FUN a function that is used to aggregate CID for each variable. The default mean will

obtain the CID as defined in Leonelli and Varando (2023).

## Value

A list with components:

- wrong a stages-like structure which record where object2 wrongly infer the interventional distance with respect to object1.
- cid the value of the computed CID.

#### References

Leonelli M., Varando G. *Context-Specific Causal Discovery for Categorical Data Using Staged Trees*, The 26th International Conference on Artificial Intelligence and Statistics (AISTATS), 2023, https://arxiv.org/abs/2106.04416

```
model1 <- stages_bhc(full(Titanic))
model2 <- stages_bhc(full(Titanic,
   order = c("Survived", "Sex", "Age", "Class")
))
cid(model1, model2)$cid
cid(model1, model2)$wrong</pre>
```

ci\_matrices 11

ci\_matrices

Conditional independences matrices of stages

## **Description**

Generate the sequence of all the conditional independences matrices of stages for a given variable in the model.

## Usage

```
ci_matrices(object, var)
```

## Arguments

object an object of class sevt.

var string, the name of one of the variables in object.

#### Value

A list with i-1 matrices, where i is the depth of variable var in the tree.

## **Examples**

compare\_stages

Compare two staged event tree

## **Description**

Compare two staged event trees, return the differences of the stages structure and plot the difference tree. Three different methods to compute the difference tree are available (see Details).

12 compare\_stages

#### Usage

```
compare_stages(
  object1,
  object2,
  method = "naive",
  return_tree = FALSE,
  plot = FALSE,
  ...
)
hamming_stages(object1, object2, return_tree = FALSE)
diff_stages(object1, object2)
```

#### **Arguments**

```
object1 an object of class sevt.

object2 an object of class sevt.

method character, method to compare staged event trees. One of: "naive", "hamming" or "stages".

return_tree logical, if TRUE the difference tree is returned.

plot logical.

... additional parameters to be passed to plot.sevt.
```

#### **Details**

compare\_stages tests if the stage structure of two sevt objects is the same. Three methods are available:

- naive first applies stndnaming to both objects and then simply compares the resulting stage names.
- hamming uses the hamming\_stages function that finds a minimal subset of nodes which stages must be changed to obtain the same structure.
- stages uses the diff\_stages function that compares stages to check whether the same stage structure is present in both models.

Setting return\_tree = TRUE will return the stages difference obtained with the selected method. The stages difference is a list of numerical vectors with same lengths and structure as stages(object1) or stages(object2), where values are 1 if the corresponding node has different (with respect to the selected method) associated stage, and 0 otherwise.

With plot = TRUE the plot of the difference tree is displayed.

If return\_tree = FALSE and plot = FALSE the logical output is the same for the three methods and thus the naive method should be used since it is computationally faster.

hamming\_stages finds a minimal set of nodes for which the associated stages should be changed to obtain equivalent structures. To do that, a maximum-weight bipartite matching problem between the stages of the two staged trees is solved using the Hungarian method implemented in the solve\_LSAP function of the **clue** package. hamming\_stages requires the package clue.

confint.sevt 13

#### Value

compare\_stages: if return\_tree = FALSE, logical: TRUE if the two models are exactly equal, otherwise FALSE. Else if return\_tree = TRUE, the differences between the two trees, according to the selected method.

hamming\_stages: if return\_tree = FALSE, integer, the minimum number of situations where the stage should be changed to obtain the same models. If return\_tree = TRUE a stages-like structure showing which situations should be modified to obtain the same models.

diff\_stages: a stages-like structure marking the situations belonging to stages which are not the exactly equal.

## **Examples**

```
data("Asym")
mod1 <- stages_bhc(full(Asym, lambda = 1))
mod2 <- stages_fbhc(full(Asym, lambda = 1))
compare_stages(mod1, mod2)

##########
m0 <- full(PhDArticles[, 1:4], lambda = 0)
m1 <- stages_bhc(m0)
m2 <- stages_bj(m0, distance = "totvar", thr = 0.25)
diff_stages(m1, m2)</pre>
```

confint.sevt

Confidence intervals for staged event tree parameters

#### **Description**

Confint method for class sevt.

## Usage

```
## S3 method for class 'sevt'
confint(
  object,
  parm,
  level = 0.95,
  method = c("wald", "waldcc", "wilson", "goodman", "quesenberry-hurst"),
  ignore = object$name_unobserved,
  ...
)
```

## Arguments

object an object of class sevt.

14 confint.sevt

parm	a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
level	the confidence level required.
method	a character string specifing which method to use: wald", "waldcc", "goodman", "quesenberry-hurst" or "wilson".
ignore	vector of stages which will be ignored, by default the name of the unobserved stages stored in object\$name_unobserved.
	additional argument(s) for compatibility with confint methods.

#### **Details**

Compute confidence intervals for staged event trees. Currently five methods are available:

- wald, waldcc: Wald method and with continuity correction.
- wilson, quesenberry-hurst and goodman.

#### Value

A matrix with columns giving lower and upper confidence limits for each parameter. These will be labelled as (1-level)/2 and 1 - (1-level)/2 in % (by default 2.5% and 97.5%).

#### Author(s)

The function is partially inspired by code in the MultinomCI function from the **DescTools** package, implemented by Andri Signorelli and Pablo J. Villacorta Iglesias.

## References

Goodman, L. A. (1965) On Simultaneous Confidence Intervals for Multinomial Proportions Technometrics, 7, 247-254.

Wald, A. Tests of statistical hypotheses concerning several parameters when the number of observations is large, Trans. Am. Math. Soc. 54 (1943) 426-482.

Wilson, E. B. Probable inference, the law of succession and statistical inference, J.Am. Stat. Assoc. 22 (1927) 209-212.

Quesenberry, C., & Hurst, D. (1964). Large Sample Simultaneous Confidence Intervals for Multinomial Proportions. Technometrics, 6(2), 191-195

```
m1 <- stages_bj(full(PhDArticles), distance = "kullback", thr = 0.01)
confint(m1, "Prestige", level = 0.90)
confint(m1, "Married", method = "goodman")
confint(m1, c("Married", "Kids"))</pre>
```

covid\_patients 15

covid\_patients

Trajectories of hospitalized SARS-CoV-2 patients

## **Description**

Dataset with observations from four variables (Sex, Age, ICU, death) for 10000 simulated SARS-CoV-2 hospital patients.

#### Usage

covid\_patients

#### **Format**

A data frame with 10000 observations of 4 variables. The variables and their levels are as follows:

• Sex: Female, Male

• Age: 0-39, 40-49, 50-59, 60-69, 70-79, 80+

ICU: yes, nodeath: yes, no

#### **Details**

The data are simulated from an event tree where conditional probabilities for ICU and death are taken from the results of Lefrancq et al. (2021). Lefrancq et al. (2021) estimated such probabilities from data on patients, recorded in the SI-VIC database, who started their hospitalization between 13 March and 30 November 2020.

#### **Source**

The data has been generated with the code in the Examples section. Conditional probabilities were copied from the tables in the Supplementary materials of Lefrancq et al. (2021). Marginal probabilities of gender and probabilities of age given gender were instead obtained from the linked GitHub repository https://github.com/noemielefrancq/Evolution-Outcomes-COVID19-France.

#### References

Leonelli, M. and Varando, G. (2023). Context-Specific Causal Discovery for Categorical Data Using Staged Trees. *Proceedings of The 26th International Conference on Artificial Intelligence and Statistics*, in *Proceedings of Machine Learning Research* 206:8871-8888 Available from https://proceedings.mlr.press/v206/lea

Lefrancq N., Paireau J., Hozé N., Courtejoie N., Yazdanpanah Y., Bouadma L. (2021). Evolution of outcomes for patients hospitalised during the first 9 months of the SARS-CoV-2 pandemic in France: A retrospective national surveillance data analysis. *The Lancet Regional Health - Europe*, 5:100087.

16 covid\_patients

```
library(stagedtrees)
data_model <- sevt(list(</pre>
 Sex = c("Female", "Male"),
 Age = c(
    "0-39", "40-49", "50-59", "60-69",
    "70-79", "80+"
 ),
 ICU = c("yes", "no"),
 death = c("yes", "no")
), full = TRUE)
data_model$prob <- list()</pre>
data_model\prob$Sex <- list("1" = c(Female = 0.45185, Male = 0.54815))
dist_age_male <- c(</pre>
 0.01616346, # 0 - 39
 0.04159445, # 40 - 49
 0.10130439, # 50 - 59
 0.16825686, # 60 - 69
 0.25217550, # 70 - 79
 0.42050534
) # 80+
dist_age_female <- c(</pre>
 0.01688613, # 0 - 39
 0.04271329, # 40 - 49
 0.10131681, # 50 - 59
 0.16841872, # 60 - 69
 0.25289366, # 70 - 79
 0.41777138
) # 80+
names(dist_age_male) <- data_model$tree$Age</pre>
names(dist_age_female) <- data_model$tree$Age</pre>
data_model$prob$Age <- list(</pre>
  "1" = dist_age_female,
 "2" = dist_age_male
)
data_model$prob$ICU <- list(</pre>
 "1" = c(yes = 0.125, no = 1 - 0.125), # Female 0-39
 "2" = c(yes = 0.149, no = 1 - 0.149), # Female 40-49
 "3" = c(yes = 0.193, no = 1 - 0.193), # Female 50-59
 "4" = c(yes = 0.225, no = 1 - 0.225), # Female 60-69
 "5" = c(yes = 0.175, no = 1 - 0.175), # Female 70-79
 "6" = c(yes = 0.037, no = 1 - 0.037), # Female 80+
 "7" = c(yes = 0.197, no = 1 - 0.197), # Male 0-39
  "8" = c(yes = 0.2687, no = 1 - 0.2687), # Male 40-49
  "9" = c(yes = 0.3171, no = 1 - 0.3171), # Male 50-59
 "10" = c(yes = 0.3415, no = 1 - 0.3415), # Male 60-69
 "11" = c(yes = 0.274, no = 1 - 0.274), # Male 70-79
 "12" = c(yes = 0.073, no = 1 - 0.073) # Male 80+
```

depsubtree 17

```
data_model$prob$death <- list(</pre>
 "1" = c(yes = 0.077, no = 1 - 0.077), # Female 0-39 ICU
 "2" = c(yes = 0.004, no = 1 - 0.004), # Female 0-39 no-ICU
 "3" = c(yes = 0.117, no = 1 - 0.117), # Female 40-49 ICU
 "4" = c(yes = 0.017, no = 1 - 0.017), # Female 40-49 no-ICU
 "5" = c(yes = 0.185, no = 1 - 0.185), # Female 50-59 ICU
 "6" = c(yes = 0.030, no = 1 - 0.030), # Female 50-59 no-ICU
 "7" = c(yes = 0.239, no = 1 - 0.239), # Female 60-69 ICU
 "8" = c(yes = 0.058, no = 1 - 0.058), # Female 60-69 no-ICU
 "9" = c(yes = 0.324, no = 1 - 0.324), # Female 70-79 ICU
 "10" = c(yes = 0.124, no = 1 - 0.124), # Female 70-79 no-ICU
 "11" = c(yes = 0.454, no = 1 - 0.454), # Female 80+ ICU
 "12" = c(yes = 0.266, no = 1 - 0.266), # Female 80+ no-ICU
 "13" = c(yes = 0.079, no = 1 - 0.079), # Male 0-39 ICU
 "14" = c(yes = 0.008, no = 1 - 0.008), # Male 0-39 no-ICU
 "15" = c(yes = 0.098, no = 1 - 0.098), # Male 40-49 ICU
 "16" = c(yes = 0.016, no = 1 - 0.016), # Male 40-49 no-ICU
 "17" = c(yes = 0.171, no = 1 - 0.171), # Male 50-59 ICU
 "18" = c(yes = 0.030, no = 1 - 0.030), # Male 50-59 no-ICU
 "19" = c(yes = 0.278, no = 1 - 0.278), # Male 60-69 ICU
 "20" = c(yes = 0.067, no = 1 - 0.067), # Male 60-69 no-ICU
 "21" = c(yes = 0.383, no = 1 - 0.383), \# Male 70-79 ICU
 "22" = c(yes = 0.150, no = 1 - 0.150), # Male 70-79 no-ICU
 "23" = c(yes = 0.478, no = 1 - 0.478), # Male 80+ ICU
 "24" = c(yes = 0.363, no = 1 - 0.363) # Male 80+ no-ICU
)
# covid_patients <- sample_from(data_model, 10000, seed = 123)</pre>
# usethis::use_data(covid_patients, overwrite = TRUE)
```

depsubtree

Extract dependency subtree

## **Description**

Extract the dependency subtree of a staged tree with respect to a variable

## Usage

```
depsubtree(object, var, other_stages = c("NA", "indep", "full"))
```

## **Arguments**

```
object an object of class sevt.
```

var the name of one of the variable of the staged event tree.

other\_stages how to set stages for other variables (if any).

18 full\_indep

#### **Details**

The dependency sub-tree is a staged event tree which is sufficient to describe the conditional distribution of the variable var given its predecessors in the original tree represented by object. In particular the preceding variables are restricted to the parents of var in the minimal-DAG obtained with as\_parentslist. This is the minimal set of variables which contexts are sufficient to fully represent the conditional distribution of var. Stages for variables different from var are either set to NA, or to the full or indep model, depending on other\_stages.

#### Value

an object of class sevt representing the dependency sub-tree.

## **Examples**

```
mod <- stages_kmeans(full(Titanic), k = 2)
par(mfrow = c(1, 2))
plot(mod, main = "staged tree")
plot(depsubtree(mod, "Age"), main = "dependency subtree for Age")
par(mfrow = c(1, 1))</pre>
```

full\_indep

Full and independent staged event tree

#### **Description**

Build fitted staged event tree from data.

#### Usage

```
full(
   data,
   order = NULL,
   join_unobserved = TRUE,
   lambda = 0,
   name_unobserved = "UNOBSERVED"
)

## S3 method for class 'table'
full(
   data,
   order = names(dimnames(data)),
   join_unobserved = TRUE,
   lambda = 0,
   name_unobserved = "UNOBSERVED"
)

## S3 method for class 'data.frame'
```

full\_indep 19

```
full(
  data,
  order = colnames(data),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)
indep(
  data,
 order = NULL,
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)
## S3 method for class 'table'
indep(
  data,
  order = names(dimnames(data)),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)
## S3 method for class 'data.frame'
indep(
  data,
  order = colnames(data),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)
```

## Arguments

```
data data to create the model, data.frame or table.

order character vector, order of variables.

join_unobserved logical, if situations with zero observations should be joined (default TRUE).

lambda smoothing coefficient (default 0).

name_unobserved name to pass to join_unobserved.
```

#### **Details**

Functions to create full or independent staged tree models from data. The full (or saturated) staged tree is the model where every situation is in a different stage, and thus the model has the maximum

number of parameters. Conversely, the independent staged tree (indep) assigns all the situations related to the same variable to the same stage, thus it is equivalent to the independence factorization.

## **Examples**

20

```
## full model
DD <- generate_xor_dataset(4, 100)
model_full <- full(DD, lambda = 1)
## independence model (data.frame)
DD <- generate_xor_dataset(4, 100)
model <- indep(DD, lambda = 1)
model</pre>
```

generate\_linear\_dataset

Generate a random binary dataset for classification

## **Description**

Randomly generate a simple classification problem.

## Usage

```
generate_linear_dataset(
  p,
  n,
  eps = 1.2,
  gamma = runif(1, min = -p, max = p),
  alpha = runif(p, min = -p, max = p)
)
```

## Arguments

```
p number of variables.
n number of observations.
eps noise.
gamma numeric.
alpha numeric vector of length n.
```

#### Value

A data.frame with n independent random variables and one class variable C computed as sign(sum(x \* alpha) + runif(1, -eps, eps) + gamma).

```
DD <- generate_linear_dataset(p = 5, n = 1000)
```

```
generate_random_dataset
```

Generate a random binary dataset

## **Description**

Randomly generate a data.frame of independent binary variables.

## Usage

```
generate_random_dataset(p, n)
```

## **Arguments**

p number of variables.n number of observations.

#### Value

A data.frame with n independent random variables.

## **Examples**

```
DD <- generate_random_dataset(p = 5, n = 1000)
```

```
generate_xor_dataset
Generate a xor dataset
```

## **Description**

Generate a xor dataset

## Usage

```
generate_xor_dataset(p, n, eps = 1.2)
```

## Arguments

p number of variables.n number of observations.

eps error.

#### Value

The xor dataset with n + 1 variables, where the first one is the class variable C computed as a noisy xor.

get\_stage

## **Examples**

```
DD <- generate_xor_dataset(p = 5, n = 1000, eps = 1.2)
```

get\_stage

Get stage or path

## **Description**

Utility functions to obtain stages from paths and paths from stages.

#### **Usage**

```
get_stage(object, path)
get_path(object, var, stage)
```

## Arguments

object an object of class sevt.

path character vector, the path from root or a two dimensional array where each row

is a path from root.

var character, one of the variable in the staged tree.

stage character vector, the name of the stages for which the paths should be returned.

## Value

```
get_stage returns the stage name(s) for given path(s).
get_path returns a data.frame containing the paths corresponding to the given stage(s).
```

```
model <- stages_fbhc(full(PhDArticles))
get_stage(model, c("0", "male"))
paths <- expand.grid(model$tree[2:1])[, 2:1]
get_stage(model, paths)
get_path(model, "Kids", "5")
get_path(model, "Gender", "2")
get_path(model, "Kids", c("5", "6"))</pre>
```

igraph-conversion 23

igraph-conversion **igraph** conversion

#### Description

Obtain the graph representation of a staged tree or a CEG as an object from the **igraph** package.

## Usage

```
get_edges(x, ignore = x$name_unobserved, ...)
## S3 method for class 'sevt'
get_edges(x, ignore = x$name_unobserved, ...)

get_vertices(x, ignore = x$name_unobserved, ...)

## S3 method for class 'sevt'
get_vertices(x, ignore = x$name_unobserved, ...)

## S3 method for class 'ceg'
get_edges(x, ignore = x$name_unobserved, ...)

## S3 method for class 'ceg'
get_vertices(x, ignore = x$name_unobserved, ...)

## S3 method for class 'ceg'
get_vertices(x, ignore = x$name_unobserved, ...)

## S3 method for class 'sevt'
as_igraph(x, ignore = x$name_unobserved, ...)

## S3 method for class 'ceg'
as_igraph(x, ignore = x$name_unobserved, ...)
```

#### **Arguments**

x an object of class sevt or ceg.
 ignore vector of stages which will be ignored and excluded, by default the name of the unobserved stages stored in x\$name\_unobserved.
 ... additional parameters.

## **Details**

Functions to transalte the graph structure of a sevt or ceg object to a graph object from the **igraph** package. Additional functions that extract the edge lists and the vertices are available. This can be useful, for example to plot the staged tree with **igraph** or additional packages (see the examples).

24 igraph-conversion

#### Value

for get\_edges: the edges list corresponding to the graph associated to x. for get\_vertices: the vertices list corresponding to the graph associated to x. for as.igraph: a graph object from the **igraph** package.

```
mod <- stages_bhc(full(Titanic))</pre>
get_edges(mod)
get_vertices(mod)
## Not run:
library(igraph)
library(ggraph)
####### sevt example #######
## convert to igraph object
g <- as_igraph(mod)</pre>
## plot with igraph directly
plot(g, layout = layout_with_sugiyama)
## plot with ggraph
ggraph(g, "sugiyama") +
  geom_edge_fan(
   aes(
      label = label,
      label_pos = 0.5 + runif(length(label), -0.1, 0.1)
   ),
    angle_calc = "along", show.legend = FALSE, check_overlap = FALSE,
    end_cap = circle(0.02, "npc"),
   arrow = grid::arrow(
      angle = 25,
     length = unit(0.025, "npc"),
      type = "closed"
   )
  ) +
  geom_node_point(aes(x = x, y = y, color = stage),
   size = 5,
    show.legend = FALSE
  ggforce::theme_no_axes() + coord_flip() + scale_y_reverse()
####### ceg example #######
g.ceg <- as_igraph(ceg(mod))</pre>
### igraph plotting functions can be used
plot(g.ceg, layout = layout.sugiyama)
### igraph object can be also plotted with ggplot2 and ggraph
ggraph(g.ceg, "sugiyama") +
  geom_edge_fan(
   aes(
      label = label,
      color = label,
      label_pos = 0.5 + runif(length(label), -0.1, 0.1)
   ),
```

inclusions\_stages 25

```
angle_calc = "along", show.legend = FALSE, check_overlap = FALSE,
end_cap = circle(0.02, "npc"),
arrow = grid::arrow(
    angle = 25,
    length = unit(0.025, "npc"),
    type = "closed"
    )
) +
geom_node_point(aes(x = x, y = y, color = stage), size = 3, show.legend = FALSE) +
ggforce::theme_no_axes() + coord_flip() + scale_y_reverse()
## End(Not run)
```

inclusions\_stages

Inclusions of stages

## **Description**

Display the relationship between two staged tree models over the same variables.

#### Usage

```
inclusions_stages(object1, object2)
```

## **Arguments**

```
object1 an object of class sevt.
object2 an object of class sevt.
```

## **Details**

Computes the relations between the stages structures of the two models.

The relations between stages of the same variable are stored in a data frame with three columns where each row represent a relation between a stage of the first model (s1) and a stage of the second model (s2). The relation can be one of the following: inclusion (s1 < s2 or s1 > s2; equal (s1 = s2); not-equal (s1 = s2).

#### Value

a list with inclusion relations between stage structures for each variable in the models.

```
mod1 <- stages_bhc(full(PhDArticles[, 1:5], lambda = 1))
mod2 <- stages_fbhc(full(PhDArticles[, 1:5], lambda = 1))
inclusions_stages(mod1, mod2)</pre>
```

join\_unobserved

join\_positions

join positions in a staged tree model

## **Description**

join positions in a staged tree model

## Usage

```
join_positions(model, var, s1, s2)
```

#### **Arguments**

model	an object of class sevt.
var	the name of a variable in the model.
s1	stage to join
s2	stage to join

#### **Details**

this functions works similarly to the join\_stages function in the stagedtrees package, but it also joins downstream stages to make nodes with stages s1, s2 in the same position. This function works properly only when downstream variables from var have full stages vectors.

join\_unobserved

Join situations with no observations

## Description

Join situations with no observations

## Usage

```
join_unobserved(
  object,
  fit = TRUE,
  trace = 0,
  name = "UNOBSERVED",
  scope = sevt_varnames(object)[-1],
  lambda = object$lambda
)
```

logLik.sevt 27

## Arguments

object	an object of class sevt with associated data.
fit	if TRUE update model's probabilities.
trace	if > 0 print information to console.
name	character, name for the new stage storing unobserved situations.
scope	character vector, list of variables in object.
lambda	smoothing parameter for the fitting.

#### **Details**

It takes as input a (fitted) staged event tree object and it joins, in the same stage, all the situations with zero recorded observations. Since such joining does not change the log-likelihood of the model, it is a useful (time-wise) pre-processing prior to others model selection algorithms.

Unobserved situations can be joined directly in full or indep, by setting join\_unobserved = TRUE.

#### Value

a staged event tree with at most one stage per variable with no observations. If, as default, fit=TRUE the model will be re-fitted, if fit=FALSE probabilities in the output model are not estimated.

## **Examples**

```
DD <- generate_xor_dataset(p = 5, n = 10)
model_full <- full(DD, lambda = 1, join_unobserved = FALSE)
model <- join_unobserved(model_full)
logLik(model_full)
logLik(model)
BIC(model_full, model)</pre>
```

logLik.sevt

Log-Likelihood of a staged event tree

## **Description**

Compute, or extract the log-likelihood of a staged event tree.

#### Usage

```
## S3 method for class 'sevt'
logLik(object, ...)
```

## Arguments

```
object an fitted object of class sevt.
... additional parameters (compatibility).
```

28 lr\_test

#### Value

An object of class logLik.

#### **Examples**

```
data("PhDArticles")
mod <- indep(PhDArticles)
logLik(mod)</pre>
```

lr\_test

Likelihood Ratio Test for staged trees models

## Description

Function to perform likelihood ratio test between two or multiple staged event tree models.

## Usage

```
lr_test(object, ...)
```

## **Arguments**

object an object of class sevt.

... further objects of class sevt. Must specify super-models of object. See below

for details.

#### **Details**

If a single object of class sevt is passed as argument, it computes the likelihood-ratio test with respect to the independence model. If multiple objects are passed, likelihood-ratio tests between the first object and the followings are computed. In the latter case the function checks automatically if the first model is nested in the additional ones, via inclusions\_stages, and throws an error if not.

#### Value

An object of class anova which contains the log-likelihood, degrees of freedom, difference in degrees of freedom, likelihood ratio statistics and corresponding p values.

```
data(PhDArticles)
order <- c("Gender", "Kids", "Married", "Articles")
phd.mod1 <- stages_hc(indep(PhDArticles, order))
phd.mod2 <- stages_hc(full(PhDArticles, order))
## compare two nested models
lr_test(phd.mod1, phd.mod2)</pre>
```

PhDArticles 29

```
## compare a single model vs the independence model
lr_test(phd.mod1)
```

**PhDArticles** 

PhD Students Publications

## **Description**

Number of publications of 915 PhD biochemistry students during the 1950's and 1960's.

## Usage

**PhDArticles** 

## **Format**

A data frame with 915 rows and 6 variables:

**Articles** Number of articles during the last 3 years of PhD: either  $\emptyset$ , 1-2 or >2.

Gender male or female.

**Kids** yes if the student has at least one kid 5 or younger, no otherwise.

Married yes or no.

**Mentor** Number of publications of the student's mentor: low between 0 and 3, medium between 4 and 10, high otherwise.

**Prestige** low if the student is at a low-prestige university, high otherwise.

#### **Source**

The data has been modified from the Rchoice package.

#### References

Long, J. S. (1990). The origins of sex differences in science. Social Forces, 68(4), 1297-1316.

30 plot.ceg

plot.ceg

igraph's plotting for CEG

#### **Description**

```
igraph's plotting for CEG
```

## Usage

```
## S3 method for class 'ceg'
plot(x, col = NULL, ignore = x$name_unobserved, layout = NULL, ...)
```

## **Arguments**

```
x an object of class ceg.
col colors specification see plot.sevt.
ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in x$name_unobserved.
layout an igraph layout.
... additional arguments passed to plot.igraph.
```

## **Details**

This function is a simple wrapper around **igraph**'s plot.igraph. The ceg object is converted to an igraph object with as\_igraph. If not specified, the default layout used is a rotated layout.sugiyama.

We use palette() as palette for the **igraph** plotting, while plot.igraph uses as default a different palette. This is to allow matching stages colors between plot.ceg and plot.sevt.

```
## Not run:
model <- stages_bhc(full(Titanic))
model.ceg <- ceg(model)
plot(model.ceg, edge.arrow.size = 0.1, vertex.label.dist = -2)
## End(Not run)</pre>
```

plot.sevt 31

plot.sevt

Plot method for staged event trees

## **Description**

Plot method for staged event tree objects. It allows easy plotting of staged event trees with some options (see Examples).

## Usage

```
## S3 method for class 'sevt'
plot(
  Х,
  y = 10,
  limit = y,
  xlim = c(0, 1),
 ylim = c(0, 1),
 main = NULL,
  sub = NULL,
  asp = 1,
  cex_label_nodes = 0,
  cex_label_edges = 1,
  cex_nodes = 2,
  cex_tree_y = 0.9,
  col = NULL,
  col_edges = "black",
  var_names = TRUE,
  ignore = x$name_unobserved,
  pch_nodes = 16,
  lwd_nodes = 1,
  lwd_edges = 1,
)
make_stages_col(x, col = NULL, ignore = x$name_unobserved, limit = NULL)
```

## **Arguments**

```
x an object of class sevt.

y alias for limit for compatibility with plot.

limit maximum number of variables plotted.

xlim the x limits (x1, x2) of the plot.

ylim the y limits of the plot.

main an overall title for the plot.

sub a sub title for the plot.
```

32 plot.sevt

the y/x aspect ratio. asp cex\_label\_nodes the magnification to be used for the node labels. If set to 0 (as default) node labels are not showed. cex\_label\_edges the magnification for the edge labels. If set to 0 edge labels are not displayed. the magnification for the nodes of the tree. cex\_nodes the magnification for the tree in the vertical direction. Default is 0.9 to leave cex\_tree\_y some space for the variable names. col color mapping for stages, one of the following: NULL (color will be assigned based on the current palette); a named (variables) list of named (stages) vectors of colors; the character "stages", in which case the stage names will be used as colors; a function that takes as input a vector of stages and output the corresponding colors. Check the provided examples. The function make\_stages\_col is used internally and make\_stages\_col(x, NULL) or make\_stages\_col(x, "stages") can be used as a starting point for colors tweaking. col\_edges color for the edges. logical, if variable names should be added to the plot, otherwise variable names var\_names can be added manually using text.sevt. ignore vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in x\$name\_unobserved. either an integer specifying a symbol or a single character to be used as the pch\_nodes default in plotting nodes shapes see points.

# lwd\_nodes the line width for edges, a positive number, defaulting to 1. lwd\_edges the line width for nodes, a positive number, defaulting to 1.

... additional graphical parameters to be passed to points, lines, title, text and

plot.window.

```
data("PhDArticles")
mod <- stages_bj(full(PhDArticles, join_unobserved = TRUE))
### simple plotting
plot(mod)
### labels in nodes
plot(mod, cex_label_nodes = 1, cex_nodes = 0)
### reduce nodes size
plot(mod, cex_nodes = 0.5)
### change line width and nodes style
plot(mod, lwd_edges = 3, pch_nodes = 5)
### changing palette
plot(mod, col = function(s) heat.colors(length(s)))</pre>
```

Pokemon 33

```
### or changing global palette
palette(hcl.colors(10, "Harmonic"))
plot(mod)
palette("default") ##
### forcing plotting of unobserved stages
plot(mod, ignore = NULL)
### use function to specify colors
plot(mod, col = function(stages) {
  hcl.colors(n = length(stages))
### manually give stages colors
### as an example we will assign colors only to the stages of two variables
### Gender (one stage named "1") and Mentor (six stages)
col <- list(</pre>
  Gender = c("1" = "blue"),
  Mentor = c(
    "UNOBSERVED" = "grey",
    "2" = "red",
    "3" = "purple",
    "10" = "pink",
    "18" = "green",
    "22" = "brown"
  )
)
### by setting ignore = NULL we will plot also the UNOBSERVED stage for Mentor
plot(mod, col = col, ignore = NULL)
```

Pokemon

Pokemon Go Users

## **Description**

Demographic information of a population of possible Pokemon Go users.

## Usage

Pokemon

## Format

A data frame with 999 rows and 5 variables:

Use Y if the individual used the app, N otherwise

Age >30 if the individual is older than 30, <=30 otherwise

Degree Yes if the individual completed a Higher Education degree, No otherwise

34 predict.sevt

#### Gender Male or Female

**Activity** Yes if the individual was physically active (i.e. had a walk longer than 30 mins, went for a run or had a bike ride to get some exercise) in the past week before the experiment, No otherwise

#### Source

```
https://osf.io/xy5g6/
```

#### References

Gabbiadini, Alessandro, Christina Sagioglou, and Tobias Greitemeyer. "Does Pokémon Go lead to a more physically active life style?." *Computers in Human Behavior* 84 (2018): 258-263.

predict.sevt

Predict method for staged event tree

## **Description**

Predict class values from a staged event tree model.

## Usage

```
## S3 method for class 'sevt'
predict(object, newdata = NULL, class = NULL, prob = FALSE, log = FALSE, ...)
```

#### **Arguments**

object an object of class sevt with fitted probabilities.

newdata the newdata to perform predictions

class character, the name of the variable to use as the class variable, if NULL the first

element names(object\$tree) will be used.

prob logical, if TRUE the probabilities of class are returned

log logical, if TRUE log-probabilities are returned

... additional parameters, see details

#### **Details**

Predict the most probable a posterior value for the class variable given all the other variables in the model. Ties are broken at random and if, for a given vector of predictor variables, all conditional probabilities are 0, NA is returned.

if prob = TRUE, a matrix with number of rows equals to the number of rows in the newdata and number of columns as the number of levels of the class variable is returned. if log = TRUE, log-probabilities are returned.

if prob = FALSE, a vector of length as the number of rows in the newdata with the level with higher estimated probability for each new observations is returned.

print.sevt 35

#### Value

A vector of predictions or the corresponding matrix of probabilities.

## **Examples**

```
DD <- generate_xor_dataset(p = 4, n = 600)
order <- c("C", "X1", "X2", "X3", "X4")
train <- DD[1:500, order]
test <- DD[501:600, order]
model <- full(train)
model <- stages_bhc(model)
pr <- predict(model, newdata = test, class = "C")
table(pr, test$C)
# class values:
predict(model, newdata = test, class = "C")
# probabilities:
predict(model, newdata = test, class = "C", prob = TRUE)
# log-probabilities:
predict(model, newdata = test, class = "C", prob = TRUE, log = TRUE)</pre>
```

print.sevt

Print a staged event tree

## **Description**

Print a staged event tree

#### Usage

```
## S3 method for class 'sevt'
print(x, ..., max = 5)
```

#### **Arguments**

```
x an object of class sevt.
... additional parameters (compatibility).
max integer, limit on the numebr of variables to print.
```

#### **Details**

The order of the variables in the staged tree is printed (from root). In addition the number of levels of each variable is shown in square brackets. If available the log-likelihood of the model is printed.

#### Value

An invisible copy of x.

36 prob

## **Examples**

```
DD <- generate_xor_dataset(5, 100)
model <- full(DD, lambda = 1)
print(model)</pre>
```

prob

Probabilities for a staged event tree

## **Description**

Compute (marginal and/or conditional) probabilities of elementary events with respect to the probability encoded in a staged event tree.

## Usage

```
prob(object, x, conditional_on = NULL, log = FALSE, na0 = TRUE)
```

## Arguments

object an object of class sevt with probabilities.

x the vector or data.frame of observations.

conditional\_on named vector, the conditioning event.

log logical, if TRUE log-probabilities are returned.

na0 logical, if NA should be converted to 0.

#### **Details**

Computes probabilities related to a vector or a data frame of observations.

Optionally, conditional probabilities can be obtained by specifying the conditioning event in conditional\_on. This can be done either with a single named vector or with a data.frame object with the same number of rows of x. In the former, the same conditioning is used for all the computed probabilities (if x has multiple rows); while with the latter different conditioning events (but on the same variables) can be specified for each row of x.

#### Value

the probabilities to observe each observation in x, possibly conditional on the event(s) in conditional\_on.

```
data(Titanic)
model <- full(Titanic, lambda = 1)
samples <- expand.grid(model$tree[c(1, 4)])
pr <- prob(model, samples)
## probabilities sum up to one
sum(pr)
## print observations with probabilities</pre>
```

random\_parentslist 37

```
print(cbind(samples, probability = pr))

## compute one probability
prob(model, c(Class = "1st", Survived = "Yes"))

## compute conditional probability
prob(model, c(Survived = "Yes"), conditional_on = c(Class = "1st"))

## compute conditional probabilities with different conditioning set
prob(model, data.frame(Age = rep("Adult", 8)),
    conditional_on = expand.grid(model$tree[2:1])
)

## the above should be the same as
summary(model)$stages.info$Age
```

random\_parentslist

Generate a random parentslist object (DAG)

#### **Description**

generate a random DAG coded as parentslist object.

## Usage

```
random_parentslist(n, k = 2, maxp = n)
```

## **Arguments**

n number of variables.

k maximum number of levels for each variable.

maxp maximum cardinality of parents sets.

#### **Details**

For each variable a subset of random cardinality (maximum maxp) of the preceding variables is randomly selected as parents set. The possible levels of each variables are randomly selected in  $2, \ldots, k$ .

#### Value

```
a parentslist object.
```

#### **Examples**

```
random_parentslist(5, 3, 2)
## we can generate the associated staged tree
pl <- random_parentslist(4, 2, 2)
plot(as_sevt(pl), main = as.character(pl))</pre>
```

38 random\_sevt

random\_sevt

Generate a random (fitted) sevt

## **Description**

Generate a random sevt from a DAG or a tree. Probabilities are also randomly generated.

## Usage

```
random_sevt(x, q = 0.5, rfun = rexp)
## S3 method for class 'list'
random_sevt(x, q = 0.5, rfun = rexp)
## S3 method for class 'parentslist'
random_sevt(x, q = 0.5, rfun = rexp)
## S3 method for class 'sevt'
random_sevt(x, q = 0.5, rfun = rexp)
```

#### **Arguments**

x a sevt object, a parentslist object or a list.

q probability of joining stages.

rfun a function which is used to generate random conditional probabilities associated

to each stage.

# Details

The generated staged tree is obtained by randomly joining stages with probability q.

For random\_sevt.list, x should be a list representing an event tree, same format as lists provided to sevt.list. The random generated sevt will be obtained by randomly joining stages starting from a full staged event tree.

For random\_sevt.parentslist, x should be a parentslist object representing a DAG, this could be obtained with as\_parentslist or with random\_parentslist. The random generated sevt will be obtained by randomly joining stages starting from a the staged tree equivalent to the DAG.

For random\_sevt.sevt, x should be a sevt. The random generated sevt will be obtained by randomly joining stages starting from the provided sevt object.

```
Stages (conditional) probabilities are sampled from the corresponding probability simplex by generating a vector with the user-defined function \code{rfun} and normalizing it to sum up to one.

Absolute value is applied to assure non-negativity. The default \code{rfun = rexp} induces a uniform sampling from the probability simplex.
```

rename\_stage 39

#### Value

A randomly generated fitted sevt object.

#### **Examples**

```
model_gt <- random_sevt(list(
    X = c("a", "b"), Y = c("c", "d", "e"),
    Z = c("1", "2", "3"), W = c("yes", "no")
))

## sample data from model_gt and estimate a staged tree
data <- sample_from(model_gt, 100)
model_est <- stages_bhc(full(data))

## compare true and estimated model
hamming_stages(model_gt, model_est)
compare_stages(model_gt, model_est, method = "hamming", plot = TRUE)</pre>
```

rename\_stage

Rename stage(s) in staged event tree

## **Description**

Change the name of a stage in a staged event tree.

# Usage

```
rename_stage(object, var, stage, new)
```

# Arguments

object an object of class sevt.

var name of a variable in object.

stage name of the stage to be renamed.

new name for the stage.

## **Details**

No internal checks are performed and as side effect stages can be joined, if e.g. new is equal to the name of a stage for variable var.

#### Value

a staged event tree object where stages stage have been renamed to new.

40 search\_best

sam	nle	_from
Saiii	$D \perp C$	_ 1 1 0111

Sample from a staged event tree

## **Description**

Generate a random sample from the distribution encoded in a staged event tree object.

## Usage

```
sample_from(object, size = 1, seed = NULL)
```

## **Arguments**

object an object of class sevt with fitted probabilities.

size number of observations to sample.

seed an object specifying if and how the random number generator should be initial-

ized ('seeded'). Either NULL or an integer that will be used in a call to set.seed.

#### **Details**

It samples size observations according to the transition probabilities (object\$prob) in the model.

#### Value

A data frame containing size observations from the variables in object.

## **Examples**

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
sample_from(model, 10)</pre>
```

search\_best

Optimal Order Search

#### Description

Find the optimal staged event tree with a dynamic programming approach.

```
search_best(
  data,
  alg = stages_bhc,
  search_criterion = BIC,
  lambda = 0,
  join_unobserved = TRUE,
  ...
)
```

search\_greedy 41

## Arguments

data either a data.frame or a table containing the data.

alg a function that performs stages structure estimation. Similar to stages\_bhc or stages\_hclust. The function alg must accept the argument scope.

search\_criterion the criterion minimized in the order search.

lambda numerical value passed to full.

join\_unobserved logical, passed to full.

... additional arguments, passed to alg.

#### **Details**

This function is an implementation of the dynamic programming approach of Silander and Leong (2013). If the search\_criterion is decomposable the returned model attains the best value among all possible orders.

#### Value

The estimated staged event tree model.

#### References

Silander T., Leong TY. A Dynamic Programming Algorithm for Learning Chain Event Graphs. In: Fürnkranz J., Hüllermeier E., Higuchi T. (eds) Discovery Science. DS 2013. *Lecture Notes in Computer Science*, vol 8140. Springer, Berlin, Heidelberg. 2013.

Cowell R and Smith J. Causal discovery through MAP selection of stratified chain event graphs. *Electronic Journal of Statistics*, 8(1):965–997, 2014.

#### **Examples**

search\_greedy

Greedy Order Search

## Description

Search the optimal staged event tree with a greedy heuristic.

42 sevt

#### Usage

```
search_greedy(
  data,
  alg = stages_bhc,
  search_criterion = BIC,
  lambda = 0,
  join_unobserved = TRUE,
  ...
)
```

## **Arguments**

```
data either a data.frame or a table containing the data.

alg a function that performs stages structure estimation. Similar to stages_bhc or stages_hclust. The function alg must accept the argument scope.

search_criterion the criterion minimized in the order search.

lambda numerical value passed to full.

join_unobserved logical, passed to full.

... additional arguments, passed to alg.
```

#### **Details**

The greedy approach implemented in this function iteratively adds variables to the staged tree that better improve the search\_criterion.

#### Value

The estimated staged event tree model.

## **Examples**

```
model <- search_greedy(Titanic, alg = stages_fbhc)
print(model)</pre>
```

sevt

Staged event tree (sevt) class

## **Description**

Structure and usage of S3 class sevt, used to store a staged event tree.

sevt 43

#### **Usage**

```
sevt(x, full = FALSE, order = NULL)
## S3 method for class 'table'
sevt(x, full = FALSE, order = names(dimnames(x)))
## S3 method for class 'data.frame'
sevt(x, full = FALSE, order = colnames(x))
## S3 method for class 'list'
sevt(x, full = FALSE, order = names(x))
```

## **Arguments**

x a list, a data frame or table object.

full logical, if TRUE the full model is created otherwise the independence model.

order character vector, order of the variables to build the tree, by default the order of

the variables in x.

#### **Details**

A staged event tree object is a list with components:

- tree (required): A named list with one component for each variable in the model, a character vector with the names of the levels for that variable. The order of the variables in tree is the order of the event tree.
- stages (required): A named list with one component for each variable but the first, a character vector storing the stages for the situations related to path ending in that variable.
- ctables: A named list with one component for each variable, the flat contingency table of that variable given the previous variables.
- lambda: The smoothing parameter used to compute probabilities.
- name\_unobserved: The stage name for unobserved situations.
- prob: The conditional probability tables for every variable and stage. Stored in a named list with one component for each variable, a list with one component for each stage.
- Il: The log-likelihood of the estimated model. If present, logLik.sevt will return this value instead of computing the log-likelihood.

The tree structure is never defined explicitly, instead it is implicitly defined by the list tree containing the order of the variables and the names of their levels. This is sufficient to define a complete symmetric tree where an internal node at a depth related to a variable v has a number of children equal to the cardinality of the levels of v. The stages information is instead stored as a list of vectors, where each vector is indexed as the internal nodes of the tree at a given depth.

To define a staged tree from data (data frame or table) the user can call either full or indep which both construct the staged tree object, attach the data in ctables and compute probabilities. After, one of the available model selection algorithm can be used, see for example stages\_hc, stages\_bhc or stages\_hclust. If, mainly for development, only the staged tree structure is needed (without data or probabilities) the basic sevt constructor can be used.

44 sevt\_add

#### Value

A staged event tree object, an object of class sevt.

## **Examples**

```
######## from table
model.titanic <- sevt(Titanic, full = TRUE)

######## from data frame
DD <- generate_random_dataset(p = 4, n = 1000)
model.indep <- sevt(DD)
model.full <- sevt(DD, full = TRUE)

######## from list
model <- sevt(list(
    X = c("good", "bad"),
    Y = c("high", "low")
))</pre>
```

sevt\_add

Add a variable to a staged event tree

#### Description

Return an updated staged event tree with one additional variable at the end of the tree.

#### Usage

```
sevt_add(object, var, data, join_unobserved = TRUE, useNA = "ifany")
```

## **Arguments**

object an object of class sevt.

var character, the name of the new variable to be added.

data either a data. frame or a table containing the data from the variables in object

plus var.

join\_unobserved

logical, passed to full.

whether to include NA values in the tables. Argument passed to table.

#### **Details**

This function update a staged event tree object with an additional variable. The stages structure of the new variable is initialized as in the saturated model.

#### Value

An object of class sevt representing a staged event tree model with var added as last variable.

sevt\_df 45

## **Examples**

```
model <- full(Titanic, order = c("Age", "Class"))
print(model)
model <- sevt_add(model, "Survived", Titanic)
print(model)</pre>
```

sevt\_df

Number of parameters of a staged event tree

# Description

Return the number of parameters of the model.

## Usage

```
sevt_df(x)
```

## **Arguments**

Χ

An object of class sevt.

#### Value

integer, degrees of freedom of the staged event tree.

sevt\_fit

Fit a staged event tree

## **Description**

Estimate transition probabilities in a staged event tree from data. Probabilities are estimated with the relative frequencies plus, eventually, an additive (Laplace) smoothing.

```
sevt_fit(
  object,
  data = NULL,
  lambda = NULL,
  scope = NULL,
  compute_logLik = TRUE
)
```

46 sevt\_nvar

#### **Arguments**

object an object of class sevt.

data data.frame or contingency table with observations of the variables in object.

lambda smoothing parameter or pseudocount. Default (NULL) to lambda value stored

in object. If no lambda value is stored nor provided, 0 will be used with a

warning.

scope which variable should be fitted. Default (NULL) to all variables in the model. A

partial re-fit is possible only for model which are already fitted and in that case

the provided lambda will be ignored if different from object\$lambda.

compute\_logLik logical value. If TRUE the log-likelihood of the model is computed and stored.

#### **Details**

The data in form of contingency tables and the log-likelihood of the model is (eventually) stored in the returned staged event tree. Partial re-fit of a model can be performed with the scope argument. Partial re-fit can only be done over a fully fitted model, e.g. when changing the stages structure of one of the variables. In case of a partial re-fit, the data and lambda arguments will be ignored and the data and lambda value stored in the sevt object will be used (a warning is issued if such arguments are supplied).

#### Value

A fitted staged event tree, that is an object of class sevt with ctables and prob components. Additionally the chosen lambda is stored in the returned object and eventually the log-likelihood of the model is saved in the 11 field.

## **Examples**

```
########
model <- sevt(list(
    X = c("good", "bad"),
    Y = c("high", "low")
))
D <- data.frame(
    X = c("good", "good", "bad"),
    Y = c("high", "low", "low")
)
model.fit <- sevt_fit(model, data = D, lambda = 1)</pre>
```

sevt\_nvar

Number of variables

## Description

Utility returning the number of variables in a staged event tree model.

sevt\_simplify 47

#### Usage

```
sevt_nvar(object)
```

#### **Arguments**

object

An object of class sevt.

#### Value

integer, the number of variables.

sevt\_simplify

Simplify a staged tree model

# **Description**

Function to simplify a staged tree model.

## Usage

```
sevt_simplify(object, fit = TRUE)
```

# Arguments

object an object of class sevt

fit logical, if TRUE refit the model after simplification.

## **Details**

The simplify function will produce the corresponding simple staged tree, that is a staged tree where stages and positions are equivalent. To do so the function ceg is used to compute positions, and then the stages' vectors are replaced with the positions' vectors. The model is the re-fitted if the input was a fitted staged tree. Despite the name, the simplified staged tree has always a number of stages greater or equal to the initial staged tree, thus it is a more complex statistical model.

#### Value

an object of class sevt representing the simplified model. The returned model will be fitted if the input model was.

#### **Examples**

```
mod <- stages_kmeans(full(Titanic), k = 2)
simpl <- sevt_simplify(mod)
plot(simpl)</pre>
```

48 stagedtrees

sevt\_varnames

Variable names

#### **Description**

Utility returning variable-names in a staged event tree model.

## Usage

```
sevt_varnames(object)
```

## **Arguments**

object

an object of class sevt.

#### Value

A character vector.

stagedtrees

Staged event trees.

#### **Description**

Algorithms to create, learn, fit and explore staged event tree models. Functions to compute probabilities, make predictions from the fitted models and to plot, analyze and manipulate staged event trees.

#### **Details**

A staged event tree is a representation of a particular factorization of a joint probability over a product space. In particular, given a vector of categorical random variables  $X1, X2, \ldots$ , a staged event tree represents the factorization  $P(X1, X2, X3, \ldots) = P(X1)P(X2|X1)P(X3|X1, X2) \ldots$  Additionally, the stages structure indicates which conditional probabilities are equal.

Model selection algorithms:

- full model full
- independence model indep
- Hill-Climbing stages\_hc
- Backward Hill-Climbing stages\_bhc
- Fast Backward Hill-Climbing stages\_fbhc
- Backward Hill-Climbing Random stages\_bhcr
- Backward joining stages\_bj
- Simple Backward Hill-Climbing stages\_simplebhc

stagedtrees 49

- Hierarchical Clustering stages\_hclust
- K-Means Clustering stages\_kmeans
- Optimal order search\_best
- Greedy order search\_greedy

#### Probabilities, log-likelihood and predictions:

- Marginal/Conditional probabilities prob
- Log-Likelihood logLik.sevt
- Predict method predict.sevt
- Confidence intervals confint.sevt

## Plot, explore and compare:

- Plot plot.sevt
- Compare compare\_stages
- Stages inclusion inclusions\_stages
- Stages info summary.sevt
- List of parents as\_parentslist
- Barplot construction barplot.sevt
- Likelihood-ratio test lr\_test
- Context-specific interventional distance cid

## Modify models:

- Join and isolate unobserved situations join\_unobserved
- Join two stages join\_stages
- Join two positions join\_positions
- Rename a stage rename\_stage

# Author(s)

Maintainer: Gherardo Varando <gherardo.varando@gmail.com> (ORCID)

Authors:

- Federico Carli
- Manuele Leonelli (ORCID)
- · Eva Riccomagno

50 stages

#### References

Collazo R. A., Görgen C. and Smith J. Q. Chain event graphs. CRC Press, 2018.

Görgen C., Bigatti A., Riccomagno E. and Smith J. Q. Discovery of statistical equivalence classes using computer algebra. *International Journal of Approximate Reasoning*, vol. 95, pp. 167-184, 2018.

Barclay L. M., Hutton J. L. and Smith J. Q. Refining a Bayesian network using a chain event graph. *International Journal of Approximate Reasoning*, vol. 54, pp. 1300-1309, 2013.

Smith J. Q. and Anderson P. E. Conditional independence and chain event graphs. *Artificial Intelligence*, vol. 172, pp. 42-68, 2008.

Thwaites P. A., Smith, J. Q. A new method for tackling asymmetric decision problems. *International Journal of Approximate Reasoning*, vol. 88, pp. 624–639, 2017.

#### See Also

Useful links:

- https://github.com/stagedtrees/stagedtrees
- Report bugs at https://github.com/stagedtrees/stagedtrees/issues

#### **Examples**

```
data("PhDArticles")
mf <- full(PhDArticles, join_unobserved = TRUE)
mod <- stages_fbhc(mf)
plot(mod)</pre>
```

stages

The stages of a staged event tree

## Description

Functions to get or set the stages of an object of class sevt.

```
stages(object)
## S3 method for class 'sevt'
stages(object)
## S3 method for class 'sevt.stgs'
print(x, ..., max = 5)
stages(object) <- value
## S3 method for class 'sevt.stgs'</pre>
```

stages 51

```
x[i, ...]
## S3 replacement method for class 'sevt.stgs'
x[i, ..., fit = TRUE] <- value
## S3 method for class 'sevt.stgs'
x[[...]]
## S3 replacement method for class 'sevt.stgs'
x[[..., fit = TRUE]] <- value</pre>
```

#### **Arguments**

object	an object of class sevt.
x	an object of class sevt.stgs (obtained by stages(object)).
	a path or context in the event tree.
max	integer, limit on the number of variables to print.
value	the stages replacement value.
i	index of variables in the tree.
fit	logical, if TRUE (default) the model will be re-fitted.

#### **Details**

This functions are the preferred way to access and modify directly the stages of an object of class sevt. In particular the indexing and replacing methods for the object extracted with the function stages() take care of checking the stages sanity and refit the object probabilities when needed. This is useful for manually setting some independence statements (see the Examples).

#### Value

For stages(): returns an object of class sevt.stgs which encode the stages of object. Objects of class sevt.stgs have dedicated method for sub-setting and replacing.

## Stages indexing

Stages can be indexed, retrieved and replaced by the corresponding variables names and/or by paths or contexts.

In particular, stages(object)[[var]] extracts the stages vector corresponding to variable var (similarly to object\$stages[[var]]. Alternatively stages(object)[[path]] indexes a stage via the corresponding path from root (similar to get\_stage); a path is recognized as such if named or if of length > 2.

stages(object)[var, context] extracts multiple stages corresponding to a variable and eventually filtered by a specific context on the preceding variables.

52 stages\_bhc

#### **Examples**

```
# start with full model
mod <- full(Titanic)</pre>
# impose the context independence Survived indep Sex, Age | Class = 1st
stages(mod)["Survived", Class = "1st"] <- "C1"</pre>
# impose Survived indep Class | Class in (2nd 3rd)
stages(mod)["Survived", Class = "3rd"] <- stages(mod)["Survived", Class = "2nd"]</pre>
# impose Age indep Class | Sex
stages(mod)["Age", Sex = "Female"] <- "S-female"</pre>
stages(mod)["Age", Sex = "Male"] <- "S-male"</pre>
# stages of Survived
stages(mod)[["Survived"]]
# stages of Survived and Age
stages(mod)[c("Survived", "Age")]
# stages of Survived in the context Class 2nd or 3rd
stages(mod)["Survived", Class = c("2nd", "3rd")]
# check independencies
as_parentslist(mod)
```

stages\_bhc

Backward hill-climbing

# Description

Greedy search of staged event trees with iterative joining of stages.

```
stages_bhc(
  object,
  score = function(x) {
    return(-BIC(x))
},
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

stages\_bhcr 53

## **Arguments**

object	an object of class sevt with fitted probabilities and data, as returned by full or ${\tt sevt\_fit}.$
score	the score function to be maximized.
max_iter	the maximum number of iterations per variable.
scope	names of variables that should be considered for the optimization.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace	if >0 increasingly amount of info is printed (via message).

## **Details**

For each variable the algorithm tries to join stages and moves to the best model that increases the score. When no increase is possible it moves to the next variable.

## Value

The final staged event tree obtained.

## **Examples**

```
DD <- generate_xor_dataset(p = 4, n = 100)
model <- stages_bhc(full(DD), trace = 2)
summary(model)</pre>
```

stages\_bhcr

Backward random hill-climbing

# Description

Randomly try to join stages. This is a pretty-useless function, used for comparisons.

```
stages_bhcr(
  object,
  score = function(x) {
    return(-BIC(x))
},
  max_iter = 100,
  trace = 0
)
```

54 stages\_bj

## **Arguments**

object an object of class sevt.

score the score function to be maximized.

max\_iter the maximum number of iteration.

trace if >0 increasingly amount of info is printed (via message).

#### **Details**

At each iteration a variable and two of its stages are randomly selected. If joining the stages increases the score, the model is updated. The procedure is repeated until the number of iterations reaches max\_iter.

#### Value

an object of class sevt.

## **Examples**

```
DD <- generate_xor_dataset(p = 4, n = 100)
model <- stages_bhcr(full(DD), trace = 2)
summary(model)</pre>
```

stages\_bj

Backward joining of stages

# Description

Join stages from more complex to simpler models using a distance and a threshold value.

## Usage

```
stages_bj(
  object,
  distance = "kullback",
  thr = 0.1,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

## **Arguments**

object an object of class sevt with fitted probabilities and data, as returned by full or

sevt\_fit.

distance character, see details.

thr the threshold for joining stages

stages\_csbhc 55

scope	names of variables that should be considered for the optimization.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace	if >0 increasingly amount of info is printed (via message).

#### **Details**

For each variable in the model stages are joined iteratively. At each iteration the two stages with minimum distance are selected and joined if their distance is less than thr.

Available distances are: manhattan (manhattan), euclidean (euclidean), Renyi divergence (reny), Kullback-Liebler (kullback), total-variation (totvar), squared Hellinger (hellinger), Bhattacharyya (bhatt), Chan-Darwiche (chandarw). See also probdist.

#### Value

The final staged event tree obtained.

## **Examples**

```
DD <- generate_xor_dataset(p = 5, n = 1000)
model <- stages_bj(full(DD, lambda = 1), trace = 2)
summary(model)</pre>
```

stages\_csbhc

Context-specific Backward hill-climbing

## **Description**

Greedy search of staged event trees with iterative joining of stages.

```
stages_csbhc(
  object,
  score = function(x) {
    return(-BIC(x$11))
},
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved
)
```

56 stages\_fbhc

# **Arguments**

object	an object of class sevt with fitted probabilities and data, as returned by full or ${\tt sevt\_fit}$ .
score	the score function to be maximized.
max_iter	the maximum number of iterations per variable.
scope	names of variables that should be considered for the optimization.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.

#### **Details**

For each variable the algorithm tries to join stages, by adding context specific independences, and moves to the best model that increases the score. When no increase is possible it moves to the next variable.

#### Value

The final staged event tree obtained.

# Examples

```
model <- stages_csbhc(full(Titanic))
summary(model)</pre>
```

stages\_fbhc

Fast backward hill-climbing

# Description

Greedy search of staged event trees with iterative joining of stages.

```
stages_fbhc(
  object,
  score = function(x) {
    return(-BIC(x))
},
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

stages\_hc 57

## **Arguments**

object	an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
score	the score function to be maximized.
max_iter	the maximum number of iteration.
scope	names of variables that should be considered for the optimization.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace	if >0 increasingly amount of info is printed (via message).

#### **Details**

For each variable the algorithm tries to join stages and moves to the first model that increases the score. When no increase is possible it moves to the next variable.

## Value

The final staged event tree obtained.

# **Examples**

```
DD <- generate_xor_dataset(p = 5, n = 100)
model <- stages_fbhc(full(DD), trace = 2)
summary(model)</pre>
```

stages\_hc

Hill-climbing

# Description

Greedy search of staged event trees with iterative moving of nodes between stages.

```
stages_hc(
  object,
  score = function(x) {
    return(-BIC(x))
},
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

58 stages\_hclust

## **Arguments**

object	an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
score	the score function to be maximized.
max_iter	the maximum number of iterations per variable.
scope	names of variables that should be considered for the optimization
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
trace	if >0 increasingly amount of info is printed (via message).

#### **Details**

For each variable node-moves that best increases the score are performed until no increase is possible. A node-move is either changing the stage associate to a node or move the node to a new stage.

The ignore argument can be used to specify stages that should not be affected during the search, that is left untouched. This is useful for preserving structural zeroes and to speed-up computations.

#### Value

The final staged event tree obtained.

## **Examples**

```
start <- indep(PhDArticles[, 1:5], join_unobserved = TRUE)
model <- stages_hc(start)</pre>
```

stages\_hclust

Learn a staged tree with hierarchical clustering

# Description

Build a stage event tree with k stages for each variable by clustering stage probabilities with hierarchical clustering.

```
stages_hclust(
  object,
  distance = "totvar",
  k = NA,
  method = "complete",
  ignore = object$name_unobserved,
  limit = length(object$tree),
  scope = NULL,
```

stages\_hclust 59

```
score = function(x) {
    return(-BIC(x))
}
)
```

# Arguments

object	an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
distance	character, the distance measure to be used, either a possible method for dist or one of the following: "totvar", "hellinger".
k	integer or (named) vector: number of clusters, that is stages per variable. Values will be recycled if needed. If NA (default) a search of the number of stage is performed with respect to the maximization of the score function. NA and integer can be mixed to fix the number of stage for some variables and use the score to select others.
method	the agglomeration method to be used in hclust.
ignore	vector of stages which will be ignored and left untouched. By default the name of the unobserved stages stored in object\$name_unobserved.
limit	the maximum number of variables to consider.
scope	names of the variables to consider.
score	A function. Score to maximize for automatic selection of the number of stages. Used if k=NA for some variables.

## **Details**

hclust\_sevt performs hierarchical clustering of the initial stage probabilities in object and it aggregates them into the specified number of stages (k). A different number of stages for the different variables in the model can be specified by supplying a (named) vector via the argument k. If k is NA for some variables, all possible number of stages will be checked and the one that maximize the score will be selected.

#### Value

A staged event tree object.

## **Examples**

```
data("Titanic")
model <- stages_hclust(full(Titanic, join_unobserved = TRUE, lambda = 1), k = 2)
summary(model)
### or search k via BIC minimization
model1 <- stages_hclust(full(Titanic), k = NA)</pre>
```

stages\_kmeans

ctage	kmeans

Learn a staged tree with k-means clustering

# Description

Build a stage event tree with k stages for each variable by clustering (transformed) probabilities with k-means.

# Usage

```
stages_kmeans(
  object,
  k = length(object$tree[[1]]),
  algorithm = "Hartigan-Wong",
  transform = sqrt,
  ignore = object$name_unobserved,
  limit = length(object$tree),
  scope = NULL,
  nstart = 1
)
```

## **Arguments**

object	an object of class sevt with fitted probabilities and data, as returned by full or $sevt\_fit.$
k	integer or (named) vector: number of clusters, that is stages per variable. Values will be recycled if needed.
algorithm	character: as in kmeans.
transform	function applied to the probabilities before clustering.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.
limit	the maximum number of variables to consider.
scope	names of the variables to consider.
nstart	as in kmeans

## **Details**

kmenas\_sevt performs k-means clustering to aggregate the stage probabilities of the initial staged tree object. Different values for k can be specified by supplying a (named) vector to k. kmeans from the stats package is used internally and arguments algorithm and nstart refer to the same arguments as kmeans.

## Value

A staged event tree.

stages\_simplebhc 61

## **Examples**

```
data("Titanic")
model <- stages_kmeans(full(Titanic, join_unobserved = TRUE, lambda = 1), k = 2)
summary(model)</pre>
```

stages\_simplebhc

Backward hill-climbing for simple staged trees

## **Description**

Greedy search of simple staged event trees with iterative joining of positions.

# Usage

```
stages_simplebhc(
  object,
  score = function(x) {
    return(-BIC(x))
},
  scope = NULL,
  max_iter = Inf,
  ignore = object$name_unobserved
)
```

# **Arguments**

object	an object of class sevt with fitted probabilities and data, as returned by full or sevt_fit.
score	the score function to be maximized.
scope	names of variables that should be considered for the optimization.
max_iter	the maximum number of iterations per variable.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in object\$name_unobserved.

#### **Details**

This function is similar to the classical backward hill-climbing implemented in stages\_bhc, but instead of joining stages it consider joining of *positions* via join\_positions. Thus, the search is in the space of simple staged tree models if the initial stage tree is simple. See the references for additional details.

#### Value

an object of class sevt, the simple staged tree resulting from the search.

62 stndnaming

#### References

Leonelli M, Varando G. Structural Learning of Simple Staged Trees, arXiv preprint arXiv:2203.04390v1

# See Also

```
join_positions() sevt_simplify()
```

# **Examples**

```
mod <- stages_simplebhc(full(Titanic))
plot(mod)</pre>
```

stndnaming

Standard renaming of stages

## **Description**

Rename all stages in a staged event tree.

## Usage

```
stndnaming(
  object,
  uniq = FALSE,
  prefix = FALSE,
  ignore = object$name_unobserved
)
```

# Arguments

object an object of class sevt.

uniq logical, if stage numbers should be unique over all tree.

prefix logical, if stage names should be prefixed with variable name.

ignore vector of stages which will be ignored and left untouched, by default the name

of the unobserved stages stored in object\$name\_unobserved.

## Value

a staged event tree object with stages named with consecutive integers.

subtree 63

#### **Examples**

```
model <- stages_fbhc(full(PhDArticles, join_unobserved = TRUE))
model$stages
model1 <- stndnaming(model)
model1$stages

### unique stage names in all tree
model2 <- stndnaming(model, uniq = TRUE)
model2$stages

### prefix stage names with variable name
model3 <- stndnaming(model, prefix = TRUE)
model3$stages

### manuallty select stage names left untouched
model4 <- stndnaming(model, ignore = c("2", "6"), prefix = TRUE)
model4$stages</pre>
```

subtree

Extract subtree

#### **Description**

Extract subtree

#### Usage

```
subtree(object, path)
```

# Arguments

object an object of class sevt.

path the path from root after which extract the subtree.

## **Details**

Returns the subtree of the staged event tree, starting from path.

## Value

A staged event tree object corresponding to the subtree.

#### **Examples**

```
DD <- generate_random_dataset(4, 100)
model <- sevt(DD, full = TRUE)
plot(model)
model1 <- subtree(model, path = c("-1", "1"))
plot(model1)</pre>
```

64 text.sevt

summary.sevt

Summarizing staged event trees

## **Description**

Summary method for class sevt.

# Usage

```
## $3 method for class 'sevt'
summary(object, ...)
## $3 method for class 'summary.sevt'
print(x, max = 10, ...)
```

## **Arguments**

object an object of class sevt.
... arguments for compatibility.
x an object of class summary.sevt.

max the maximum number of variables for which information is printed.

#### **Details**

Print model information and summary of stages.

#### Value

An object of class summary. sevt for which a print method exist.

# **Examples**

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
summary(model)</pre>
```

text.sevt

Add text to a staged event tree plot

#### **Description**

Add text to a staged event tree plot

```
## S3 method for class 'sevt' text(x, y = ylim[1], limit = 10, xlim = c(0, 1), ylim = c(0, 1), ...)
```

trajectories 65

# Arguments

x	An object of class sevt.
У	the position of the labels.
limit	maximum number of variables plotted.
xlim	graphical parameter.
ylim	graphical parameter.
	additional parameters passed to text.

trajectories

Hospital trajectories

# Description

Generated dataset with observations from five variables (SEX, AGE, ICU, RSP, OUT) describing imaginary patients' trajectories in a hospital.

#### Usage

trajectories

#### **Format**

A data frame with 10000 observations of 5 variables.

#### **Source**

The data has been generated with the code in the Examples section.

# Examples

66 trajectories

```
stages(model)["RSP", AGE = c("adult")] <- stages(model)["RSP", AGE = c("elder")]</pre>
stages(model)["OUT", AGE = "adult",
              SEX = "female",
              ICU = "1",
              RSP = c("intub", "mask")] <- "femaleICUresp"</pre>
stages(model)["OUT", AGE = "child",
                     ICU = "1",
                     RSP = "intub"] <- "childICUintub"</pre>
stages(model)["OUT", AGE = "child",
              ICU = "1",
              RSP = "mask"] <- "childICUmask"</pre>
stages(model)["OUT", AGE = "child",
              ICU = "1",
              RSP = "no"] <- "childICUno"</pre>
stages(model)["OUT", AGE = "adult", SEX = "male"] <-</pre>
 stages(model)["OUT", AGE = "elder", SEX = "female"]
stages(model)["OUT", ICU = "0", RSP = "intub"] <- "UNOBS"</pre>
stages(model)["OUT", ICU = "0", RSP = "intub"] <- "UNOBS"</pre>
stages(model)["OUT", AGE = "child", ICU = "0"] <- "UNOBS"</pre>
model$prob <- list()</pre>
model\prob\SEX \leftarrow list("NA" = c(male = 0.4, female = 0.6))
model$prob$AGE <- list("1" = c("child" = 0.1, "adult" = 0.5, "elder" = 0.4),
                       "2" = c("child" = 0.1, "adult" = 0.3, "elder" = 0.6))
"2" = c("0" = 0.4, "1" = 0.6), \# male adult
                       "5" = c("0" = 0.2, "1" = 0.8), \# female adult
                       "6" = c("0" = 0.7, "1" = 0.3)) ## elder
model$prob$RSP <- list("childnoICU" = c("intub" = NA, "mask" = NA, "no" = NA),</pre>
                       "childICU" = c("intub" = 0.1, "mask" = 0.7, "no" = 0.2),
                       "5" = c("intub" = 0, "mask" = 0.7, "no" = 0.3), # male noICU
                       "6" = c("intub" = 0.4, "mask" = 0.5, "no" = 0.1), # male ICU
                       "11" = c("intub" = 0, "mask" = 0.5, "no" = 0.5), # female noICU
                       "12" = c("intub" = 0.4, "mask" = 0.5, "no" = 0.1)) # female ICU
model$prob$OUT <- list("UNOBS" = c("death" = NA, "survived" = NA),</pre>
                       "childICUintub" = c("death" = 0.03, "survived" = 0.97),
                       "childICUmask" = c("death" = 0.02, "survived" = 0.98),
                       "childICUno" = c("death" = 0.01, "survived" = 0.99),
                       ### male adult and female elder ICU = 0 :
                       "32" = c("death" = 0.05, "survived" = 0.95), ## mask
                       "33" = c("death" = 0.01, "survived" = 0.99), ## no
```

write\_tikz 67

```
### male adult and female elder ICU = 1 :
                      "34" = c("death" = 0.15, "survived" = 0.85), ## intub
                      "35" = c("death" = 0.08, "survived" = 0.92), ## mask
                      "36" = c("death" = 0.04, "survived" = 0.96), ## no
                      #############
                      "14" = c("death" = 0.2, "survived" = 0.8), # male elder 0 mask
                      "15" = c("death" = 0.1, "survived" = 0.9), # male elder 0 no
                      "16" = c("death" = 0.3, "survived" = 0.7), # male elder 1 intub
                      "17" = c("death" = 0.25, "survived" = 0.75), # male elder 1 mask
                      "18" = c("death" = 0.3, "survived" = 0.7), # male elder 1 no
                      #############
                      "26" = c("death" = 0.1, "survived" = 0.9), # female adult 0 mask
                      "27" = c("death" = 0.15, "survived" = 0.85), # female adult 0 no
                      "30" = c("death" = 0.2, "survived" = 0.8), # female adult 1 no
                      #############
                      "femaleICUresp" = c("death" = 0.1, "survived" = 0.9)
                      )
# trajectories <- sample_from(model, 10000, seed = 1)</pre>
# usethis::use_data(trajectories, overwrite = TRUE)
```

write\_tikz

Export the staged tree or CEG graph to tikz

## Description

Generate tikz code to draw the staged tree or CEG graph.

```
write_tikz(
  layout = NULL,
  file = "",
  col = NULL,
  ignore = x$name_unobserved,
  node_label = function(node) {
     ifelse(is.na(node$stage), "", node$stage)
},
  edge_label = function(edge) {
     ifelse(is.na(edge$label), "", edge$label)
},
 edge_label_options = function(edge) {
     return("sloped")
},
  scale = 10.
  normalize_layout = TRUE,
  node_shape = "circle",
  node_inner_sep = "1mm",
```

68 write\_tikz

```
node_minimum_size = "0.3cm",
  node_draw_color = "black",
  node_thickness = "very thick",
  node_text_color = "black"
)
## S3 method for class 'sevt'
write_tikz(
 Х,
  layout = NULL,
  file = "",
  col = NULL,
  ignore = x$name_unobserved,
  node_label = function(node) {
     ifelse(is.na(node$stage), "", node$stage)
 },
  edge_label = function(edge) {
     ifelse(is.na(edge$label), "", edge$label)
 },
 edge_label_options = function(edge) {
     return("sloped")
 },
  scale = 10,
  normalize_layout = TRUE,
 node_shape = "circle",
 node_inner_sep = "1mm",
  node_minimum_size = "0.3cm",
  node_draw_color = "black",
 node_thickness = "very thick",
 node_text_color = "black"
)
```

# Arguments

х	an object of class sevt or ceg.	
layout	the layout of the graph, given as matrix with two columns and as many rows as nodes in the staged tree. By default, a modified sugiyama layout is used. The layout matrix can be obtained with <b>igraph</b> layout functions.	
file	A connection or a character string naming the file to print to. Passed to cat.	
col	color specifications for the stages of the staged even tree. Same as plot.sevt and make_stages_col.	
ignore	vector of stages which will be ignored and not plotted, by default the name of the unobserved stages stored in x\$name_unobserved.	
node_label	a function that produces nodes labels.	
edge_label	a function that produces edge labels.	
edge_label_options		
	a function that produces edge label options.	

write\_tikz 69

```
scale for the tikzfigure.

normalize_layout

a logical value. If TRUE layout positions are scaled to the [0,1] interval.

node_shape the shape to be used for nodes.

node_inner_sep the inner sep parameter.

node_minimum_size

the minimum size parameter for the nodes.

node_draw_color

the color for line drawing the nodes.

node_thickness the thickness of the lines.

node_text_color

the color for label in nodes.
```

#### **Details**

This function can be used to create a working tikz code that compile to a graph similar to the one obtained by plot.sevt(x, ...) or plot.ceg(x, ...).

#### References

Code partially inspired by the code in *Exporting graphs to LaTeX*, using igraph and TikZ http://igraph.wikidot.com/r-recipes#toc2

# **Index**

* datasets Asym, 4 covid_patients, 15	<pre>generate_xor_dataset, 21 get_edges (igraph-conversion), 23 get_path (get_stage), 22</pre>
PhDArticles, 29	get_stage, 22, 51
Pokemon, 33	get_stage, 22, 31 get_vertices (igraph-conversion), 23
trajectories, 65	get_ver tices (1graph conversion), 25
[.sevt.stgs (stages), 50	hamming_stages (compare_stages), 11
[ <sevt.stgs (stages),="" 50<="" td=""><td>hclust, 59</td></sevt.stgs>	hclust, 59
[[.sevt.stgs(stages), 50	
[[ <sevt.stgs(stages), 50<="" td=""><td>igraph-conversion, 23</td></sevt.stgs(stages),>	igraph-conversion, 23
LL sevt. stgs (stages), 50	inclusions_stages, 25, 28, 49
as.character.parentslist, 3, 7	indep, 27, 43, 48
as_adj_matrix, 5	indep (full_indep), 18
as_bn, 5	
as_igraph, 30	join_positions, 26, 49, 61
as_igraph (igraph-conversion), 23	<pre>join_positions(), 62</pre>
as_parentslist, 6, 8, 18, 38, 49	join_stages, 49
as_sevt, 7	join_unobserved, <i>19</i> , 26, <i>49</i>
Asym, 4	
,	kmeans, 60
barplot, 9	logLik, 28
barplot.sevt, 8, 49	logLik.sevt, 27, 43, 49
	1r_test, 28, 49
cat, 68	11_test, 20, 47
ceg, 9, 23, 30, 68	make_stages_col, 68
ci_matrices, 11	make_stages_col(plot.sevt), 31
cid, 10, 49	
compare_stages, 11, 49	parentslist, 37, 38
confint.sevt, 13, 49	PhDArticles, 29
covid_patients, 15	plot.ceg, 30
dencubtree 17	plot.sevt, 9, 12, 30, 31, 49, 68
depsubtree, 17	points, 32
<pre>diff_stages (compare_stages), 11 dist, 59</pre>	Pokemon, 33
uist, 39	predict.sevt, 34, 49
full, 27, 41–44, 48, 61	print.parentslist, 7
full (full_indep), 18	print.parentslist
full_indep, 18	(as.character.parentslist), 3
— · · · · · · · ·	print.sevt, 35
<pre>generate_linear_dataset, 20</pre>	print.sevt.stgs(stages),50
<pre>generate_random_dataset, 21</pre>	print.summary.sevt(summary.sevt), 64

INDEX 71

```
prob, 36, 49
probdist, 55
random_parentslist, 37, 38
random\_sevt, 38
rename_stage, 39, 49
sample_from, 40
search_best, 40, 49
search_greedy, 41, 49
sevt, 7–10, 17, 18, 23, 28, 38, 42, 43, 61, 68
sevt.list, 38
sevt_add, 44
sevt_df, 45
sevt_fit, 45, 61
sevt_nvar, 46
sevt_simplify, 47
sevt_simplify(), 62
sevt_varnames, 48
stagedtrees, 48
stagedtrees-package (stagedtrees), 48
stages, 50
stages<- (stages), 50
stages_bhc, 41-43, 48, 52, 61
stages_bhcr, 48, 53
stages_bj, 48, 54
stages_csbhc, 55
stages_fbhc, 48, 56
stages_hc, 43, 48, 57
stages_hclust, 41-43, 49, 58
stages_kmeans, 49,60
stages_simplebhc, 48, 61
stndnaming, 12, 62
subtree, 63
summary.sevt, 49, 64
table, 44
text, 65
text.sevt, 32, 64
trajectories, 65
write_tikz, 67
```